



# One Dimensional DC Mercury-Argon Fluorescent Lamp model

S. Taniguchi K. H. Loo  
H. Motomura M. Jinno

Department of Electrical and Electronic Engineering, Ehime University

Email: [stanig@mayu.ee.ehime-u.ac.jp](mailto:stanig@mayu.ee.ehime-u.ac.jp)

HP: <http://mayu.ee.ehime-u.ac.jp>



S. Taniguchi



L. Ka Hong



H. Motomura



M. Jinno

## Introduction

Mercury-Argon discharge: high efficiency UV radiation  
∴ used widely as commercial fluorescent lamp

We need plasma properties to improve lamps

Data is not enough both in experimental and theoretical way

We develop a 1 dimensional model and calculate radial distribution of Hg excited atoms to investigate plasma properties in DC Hg-Ar fluorescent lamp

## Model

•DC model

•We consider excitation and ionization for Ar. These process are not considered in past models.

•Collisional-radiative model  
•Assumption

1. Lamp is cylindrical enclosure.
2. The positive column is axially uniform.
3. The positive column is radially symmetric.
4. Electron energy distribution function is Maxwellian.
5. The number of considered excited levels are 6 for Hg and 2 for Ar.

•Basic equation

Boundary condition<sup>[1]</sup>

### Continuous equation

$$\text{Electron density } N_e: \frac{\partial N_e}{\partial t} = D_a \nabla^2 N_e + S_e$$

$$\text{Ion density } N_+: \frac{\partial N_+}{\partial t} = D_a \nabla^2 N_+ + S_+$$

$$\text{Excited atom density } N_j: \frac{\partial N_j}{\partial t} = D_e \nabla^2 N_j + S_j$$

### Energy conservation equation

$$\text{Gas temperature } T_g: \frac{3}{2} k \frac{\partial (N_{Ar} T_g)}{\partial t} = \kappa_{Ar} \nabla^2 T_g + S_{Tg}$$

Electron energy  $\bar{\varepsilon}$ :

$$\frac{\partial \bar{\varepsilon}}{\partial t} = \nabla \cdot \left( -\frac{5}{3} \mu_e E_r \bar{\varepsilon} - \frac{5}{3} D_e \nabla \bar{\varepsilon} \right) + S_{\bar{\varepsilon}}$$

### center

$$\left. \frac{\partial N_e}{\partial r} \right|_{r=0} = 0$$

$$\left. \frac{\partial N_+}{\partial r} \right|_{r=0} = 0$$

$$\left. \frac{\partial N_j}{\partial r} \right|_{r=0} = 0$$

$$\left. \frac{\partial T_g}{\partial r} \right|_{r=0} = 0$$

$$\left. \frac{\partial \bar{\varepsilon}}{\partial r} \right|_{r=0} = 0$$

### wall

$$N_e|_{r=R} = 0$$

$$N_+|_{r=R} = 0$$

$$N_j|_{r=R} = 0$$

$$T_g|_{r=R} = T_w$$

$$\bar{\varepsilon}|_{r=R} = 0$$

$k$ : Boltzmann constant  $D_a$ : ambipolar diffusion coefficient  $D_e$ : electron diffusion coefficient  $\mu_e$ : electron mobility  $\kappa_{Ar}$ : Ar thermal conductivity  $E_r$ : ambipolar electric field  $S_x$ : generation-loss term of x

$$\bar{\varepsilon} = \frac{3}{2} k N_e T_e$$

## Comparison of simulation results and references<sup>[2]</sup>

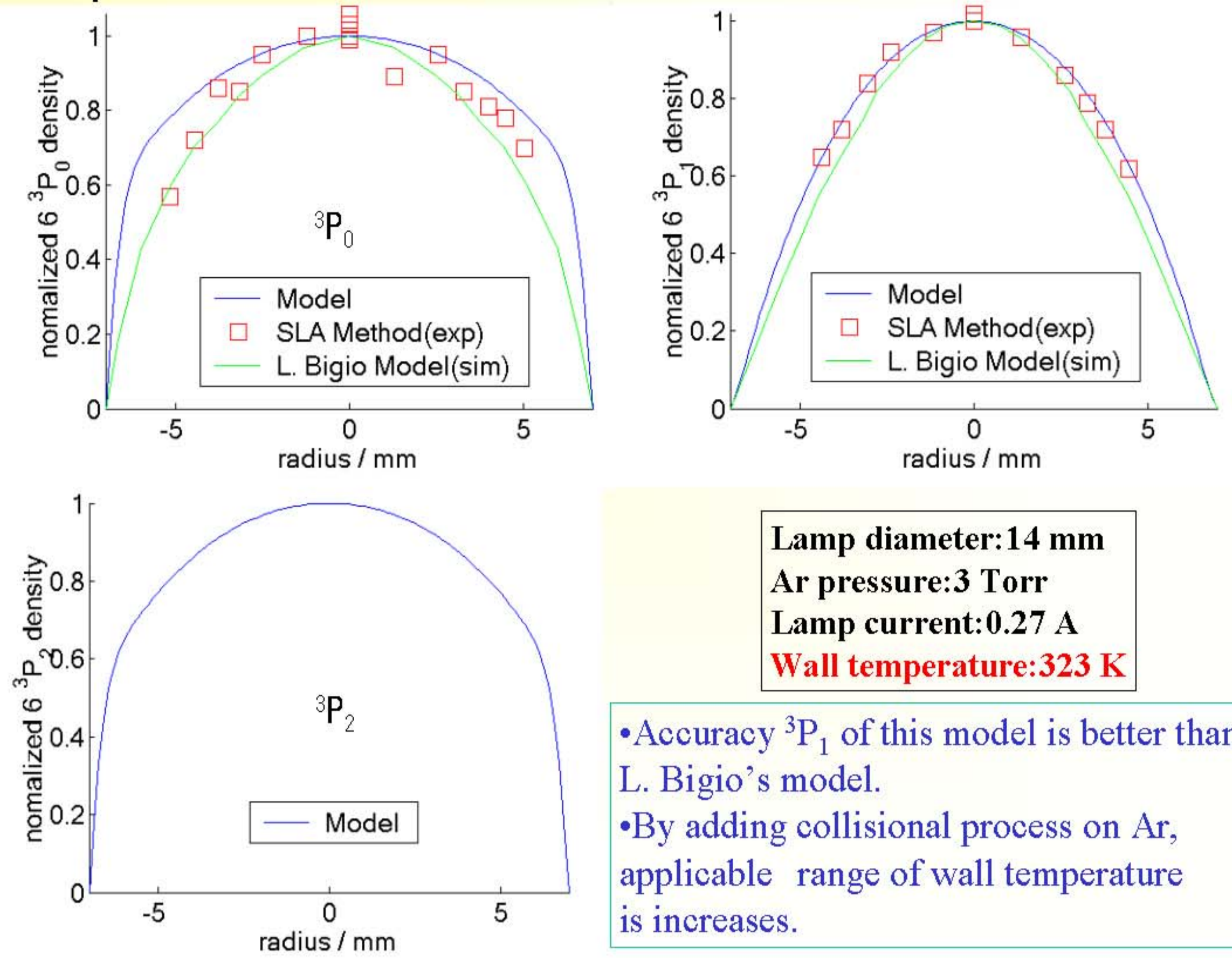


Fig.2: Comparison of  ${}^3P_j$  density from experiment and model ( $T_w=323$  K)

Lamp diameter: 14 mm  
Ar pressure: 3 Torr  
Lamp current: 0.27 A  
Wall temperature: 323 K

- Accuracy  ${}^3P_1$  of this model is better than L. Bigio's model.
- By adding collisional process on Ar, applicable range of wall temperature is increases.

## Distribution of electron density and excitation atom density

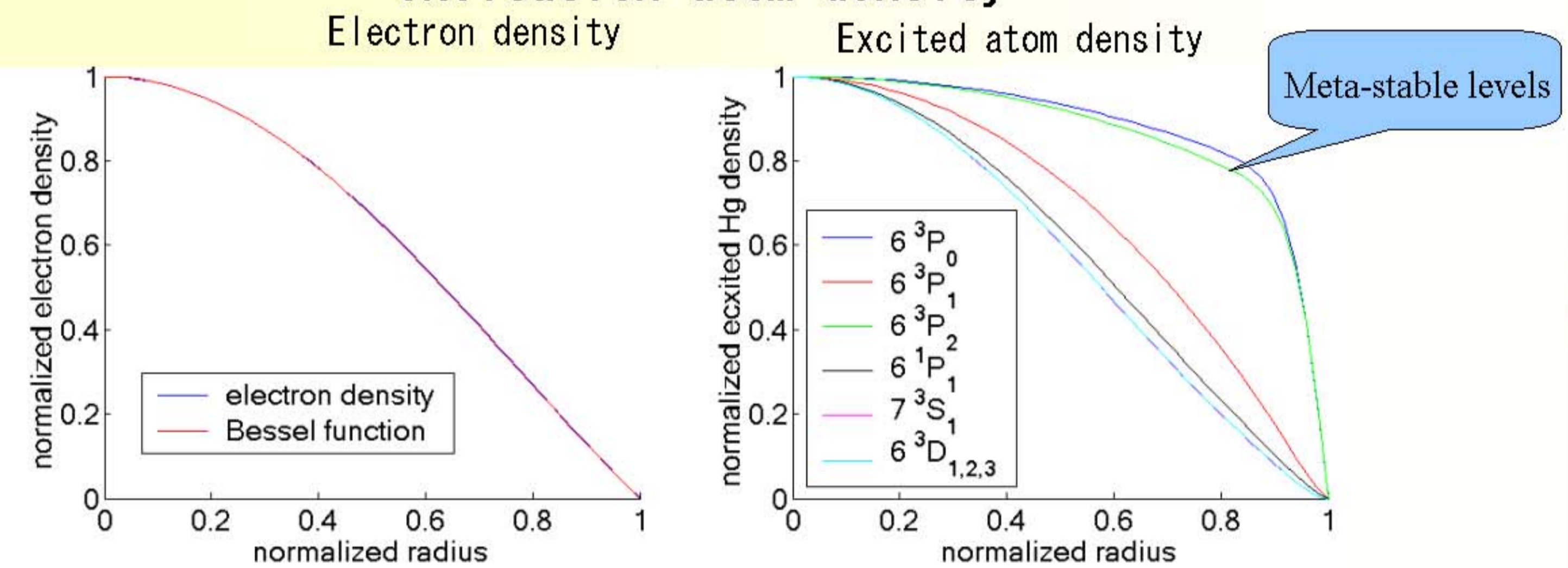


Fig.3: Electron density and mercury excited densities

Lamp diameter: 14 mm  
Ar pressure: 3 Torr  
Lamp current: 0.27 A  
Wall temperature: 313 K

Electron density distribution: Distribution matches zeroth order Bessel function very much  
Excited atom density distribution: Only meta-stable levels are broad to the wall.

Meta-stable atoms diffuse to the wall because radiation are forbidden from meta-stable.

## Meta-stable and resonance atom densities when wall temperature was changed

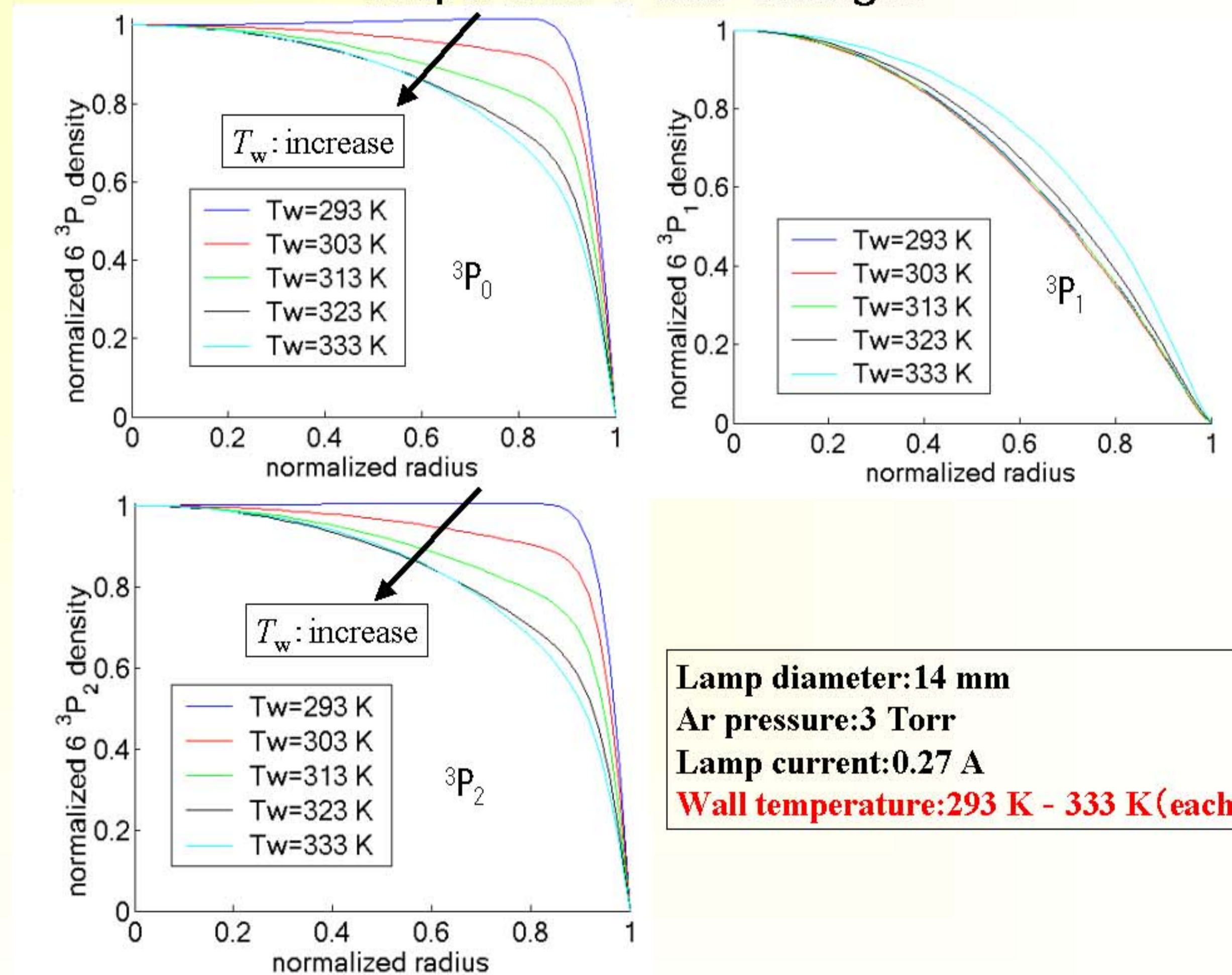


Fig.4: Meta-stable and resonance atom density when wall temperature was changed

Meta-stable level: When  $T_w$  is increase, distributions become narrow  
Resonance level: Density does not change very much until  $T_w$  is 323K

## Conclusion

We developed the model which has good agreement with experiment and show difference of excited atom distributions and of meta-stable and resonance level atom distribution dependence on wall temperature.

## Comparison of simulation results and references<sup>[2]</sup>

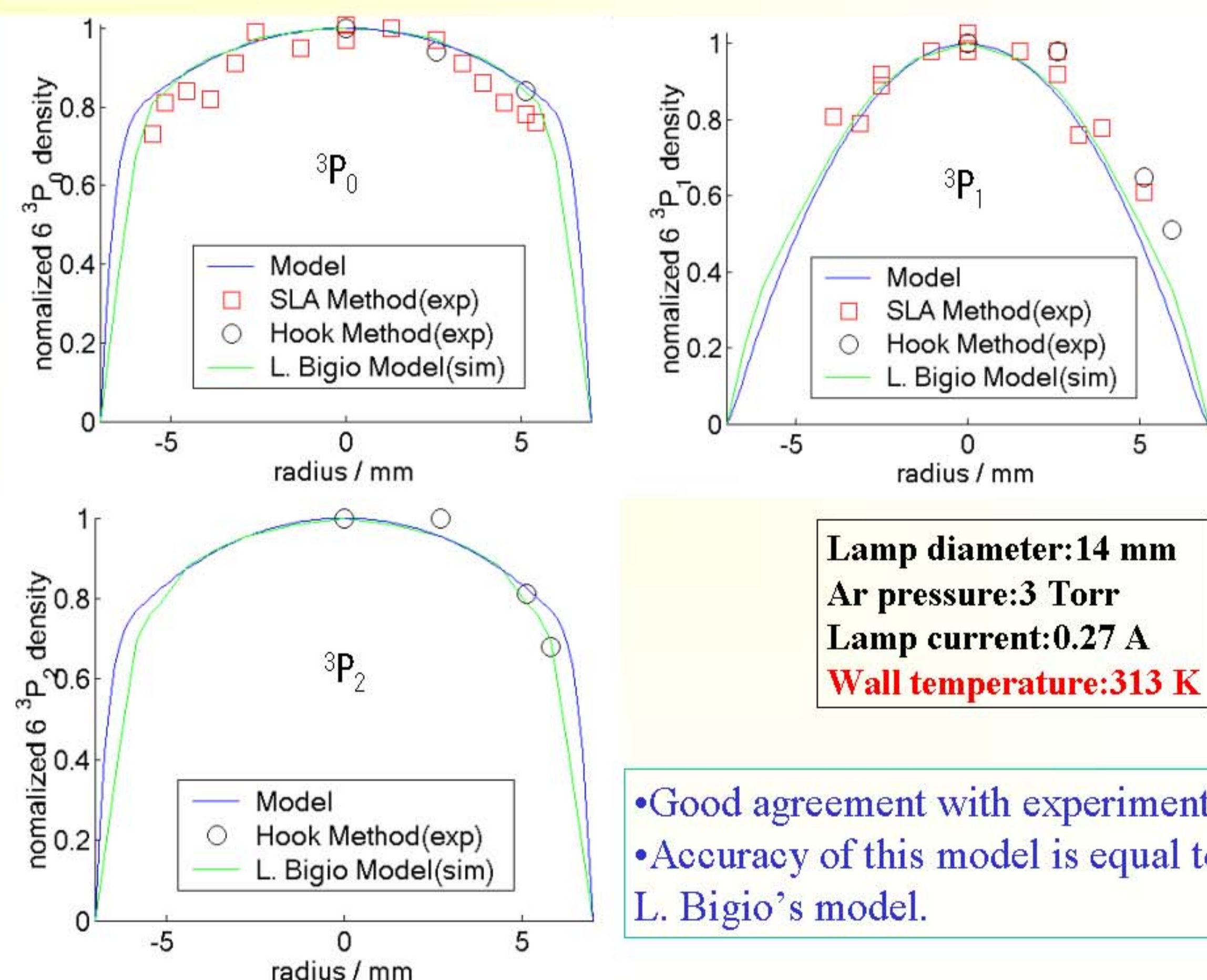


Fig. 1: Comparison of  ${}^3P_j$  density from experiment and model ( $T_w=313$  K)

Lamp diameter: 14 mm  
Ar pressure: 3 Torr  
Lamp current: 0.27 A  
Wall temperature: 313 K

- Good agreement with experimental data.
- Accuracy of this model is equal to L. Bigio's model.

## references

- [1] G. G. Lister: Computer Physics Communications, Vol. 75, p. 160 (1992)
- [2] L. Bigio et al.: Journal of Applied Physics, Vol. 65, p. 375 (1989)